

Calculus Warm Up #4-4

New team # on your WU!

Compare results using a right, left, and midpoint Riemann sum, to approximate the area under the function from yesterday's warm up.

$$\int_0^1 \sqrt{x+1} \, dx, n=4$$

from yesterday

$$\text{Actual} \approx 1.2190$$

$$\text{Simp.} \approx 1.2189$$

$$\text{Trap.} \approx 1.2182$$

HW Questions: p. 289

In Exercises 1–18, find the indefinite integral.

$$1. \int \frac{2}{3\sqrt[3]{x}} \, dx$$

$$3. \int (2x^2 + x - 1) \, dx$$

$$5. \int \frac{(1+x)^2}{\sqrt{x}} \, dx$$

$$7. \int \frac{3x^2}{\sqrt{x^3+3}} \, dx$$

$$9. \int (x^2+1)^3 \, dx$$

$$u = x^3 + 3$$

$$du = 3x^2 \, dx$$

$$= \frac{1}{3} \int u^{1/2} \, du$$

$$1x^6 + 3x^4 + 3x^2 + 1$$

HW Questions: p. 289

In Exercises 1–18, find the indefinite integral.

11. $\int x(x^2 + 1)^3 dx$

13. $\int \frac{x}{(x^2 + 1)^3} dx$

15. $\int x^2 \sqrt{x + 5} dx \longrightarrow u = x + 5 \quad du = dx$

$x = u - 5$

$x^2 = u^2 - 10u + 25$

17. $\int \frac{x^3 + 1}{x^2} dx$

$\int (x + x^{-2}) dx$

$\int (u^2 - 10u + 25) u^{1/2} du$

In Exercises 21–30, use the Fundamental Theorem of Calculus to evaluate the definite integral.

21. $\int_0^4 (2 + x) dx$

23. $\int_{-1}^1 (4t^3 - 2t) dt$

25. $\int_0^3 \frac{1}{\sqrt{1+x}} dx$

$u = 1 + x \quad du = dx$

$x = 0 \rightarrow u = 1$

$x = 3 \rightarrow u = 4$

$\int_1^4 u^{-1/2} du$

In Exercises 21–30, use the Fundamental Theorem of Calculus to evaluate the definite integral.

27. $\int_4^9 x\sqrt{x} \, dx$

$$x \cdot x^{1/2}$$

$$\int_4^9 x^{3/2} \, dx$$

29. $-2\pi \int_0^1 (y+1)\sqrt{1-y} \, dy$

Let $u = 1-y$ $du = -dy$
 $y = 1-u$ for $y=0$ $u=1$
 $y=1$ $u=0$

$$-2\pi \int_1^0 (1-u+1)\sqrt{u} \, du$$

$$2\pi \int_1^0 (u-2)u^{1/2} \, du$$

$$2\pi \int_1^0 (u^{3/2} - 2u^{1/2}) \, du$$

31. Find the function f whose derivative is $f'(x) = -2x$ and whose graph passes through the point $(-1, 1)$.

$$f(x) = \int (-2x) \, dx$$

@ $x = -1 \rightarrow 1 = -(-1)^2 + C$
 $C = 2$

$$f(x) = -x^2 + C$$

$$f(x) = -x^2 + 2$$

33. An airplane taking off from a runway travels 3600 feet before lifting off. If it starts from rest, moves with constant acceleration, and makes the run in 30 seconds, with what speed does it lift off?

$$a(t) = a \quad v(t) = \int a \, dt \quad s(t) = \int at \, dt$$

$$v(t) = at + C \quad s(t) = \frac{at^2}{2} + C$$

$$v(0) = 0 + C \quad s(0) = 0 + C$$

$$C = 0 \quad C = 0$$

$$v(t) = at \quad s(t) = \frac{at^2}{2}$$

Now • in 30 secs, distance traveled = 3600 ft:

$$s(30) = \frac{a(30)^2}{2}$$

$$3600 = \frac{a(900)}{2}$$

$$a = 8 \text{ ft/sec}^2$$

$$v(30) = 8(30)$$

$$v(30) = 240 \text{ ft/sec}$$

In Exercises 45–48, find the average value of the function over the given interval. Find the values of x where the function assumes its mean value and sketch the graph of the function.

45. $f(x) = \frac{1}{\sqrt{x-1}}$ [5, 10] 47. $f(x) = x$ [0, 4]

$$f(c) = \frac{1}{10-5} \int_5^{10} \frac{1}{\sqrt{x-1}} dx \quad u = x-1 \quad du = dx$$

$$f(c) = \frac{1}{5} \left[2(x-1)^{1/2} \right]_5^{10}$$

$$= \frac{2}{5} (3 - 2)$$

$$f(c) = \frac{2}{5}$$

$$\frac{2}{5} = \frac{1}{\sqrt{c-1}}$$

$$\sqrt{c-1} = \frac{5}{2}$$

$$c-1 = \frac{25}{4}$$

$$c = \frac{29}{4}$$

In Exercises 49 and 50, use Simpson's Rule with ($n = 4$) to approximate the definite integral.

49. $\int_1^2 \frac{1}{1+x^3} dx$ $h = \frac{2-1}{4} = \frac{1}{4}$

$$A = \frac{1}{12} [f(1) + 4f(1.25) + 2f(1.5) + 4f(1.75) + f(2)]$$

Classwork - review Ch. 5

Name _____ Team _____

Find the indefinite integrals

Per _____

1. $\int \frac{2}{\sqrt[3]{3x}} dx$

2. $\int \frac{x^3 - 2x^2 + 1}{x^2} dx$

3. $\int x^2 \sqrt{x^3 + 3} dx$

4. $\int \frac{x^2 + 2x}{(x+1)^2} dx$

$$\int \left[\frac{(x^2 + 2x + 1) - 1}{(x+1)^2} \right] dx$$

$$\int [1 - (x+1)^{-2}] dx$$

$$= x + 1 + \frac{1}{x+1} + C$$

$$= x + \frac{1}{x+1} + C$$

Find the definite integrals

5. $\int_{-1}^1 (t^2 + 2) dt$

$$\frac{14}{3}$$

6. $\int_3^6 \frac{x}{3\sqrt{x^2 - 8}} dx$

$$\frac{2\sqrt{7} - 1}{3}$$

7. $\int_0^1 x^2(x^3 + 1)^3 dx$

$$\frac{5}{4}$$

8. $\int_{-1}^{\sqrt[3]{17}} \frac{x^2}{x^3 - 1} dx$

$$\ln 2$$

9. A function f has a second derivative $f''(x) = 6(x - 1)$. Find the function if its graph passes through the point $(2, 1)$ and at that point is tangent to the line given by $3x - y - 5 = 0$. \rightarrow

$y = 3x - 5$ $f'(x) = \int (6x - 6) dx$
 @ $(2, 1)$ slope = 3 $\rightarrow f'(x) \rightarrow$

$$f(x) = (x - 1)^3$$

10. Find the c guaranteed by The Mean Value Theorem and the average value of the given function for the given interval.

$f(x) = x^3$ $[0, 2]$

$$c = \sqrt[3]{2}$$

Staple up. ☺

Classwork Week 4

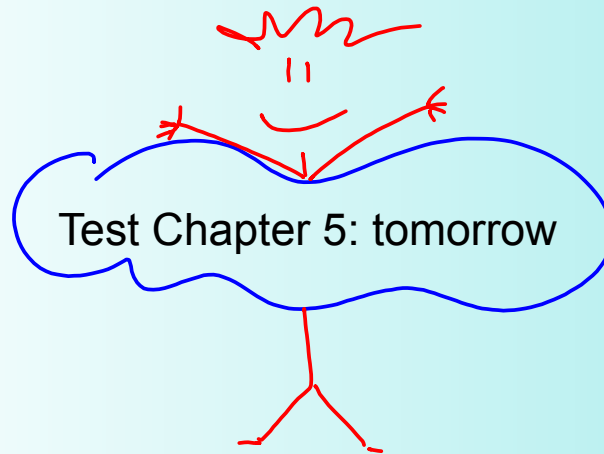
Warm Up

Pink

HW: Integration WS (blue)

Answers follow. Turn it in tomorrow!

#3 should be dt , not dx



Answers blue WS

1. $\frac{2}{9}(3x-2)^{3/2} + C$

6. $\frac{10}{3}$

2. $\frac{2}{5}(2-x)^{5/2} - 2(2-x)^{3/2} + C$

7. $\frac{4752}{35}$

3. $\frac{3}{7}(t-4)^{7/3} + 3(t-4)^{4/3} + C$

8. $\frac{10}{81}$

4. $\frac{4}{3}(x+3)^{3/2} - 14(x+3)^{1/2} + C$

5. $\frac{65}{2}$